

3-56

(GS)

+ve  
↑



↑  $\frac{g}{4}$

After  $\Delta t$ , sandbag dropped  
 Time to hit ground.

(DP) ① Calc height ascended in  $\Delta t$  ( $s = ut + \frac{1}{2}at^2$ )

② calc initial upward speed of sandbag ( $v = u + at$ )

③ Calculate time of descent ( $s = ut + \frac{1}{2}at^2$ )

(Ex)

Up

$$s = 0 + \frac{g(\Delta t)^2}{8}$$

$$v = 0 + \frac{g\Delta t}{4}$$

Down

$$u = \frac{g\Delta t}{4} \uparrow$$

↓ -g

$$-\left(\frac{g\Delta t^2}{8}\right) = \frac{g\Delta t}{4}t - \frac{1}{2}gt^2$$

$$\frac{1}{2}t^2 - \frac{\Delta t}{4}t - \frac{\Delta t^2}{8} = 0$$

$$a = \frac{1}{2} \quad b = -\frac{\Delta t}{4} \quad c = -\frac{\Delta t^2}{8}$$

$$a = 1 \quad b = -\frac{\Delta t}{2} \quad c = -\frac{\Delta t^2}{4}$$

$$t = \frac{\frac{\Delta t}{2} \pm \sqrt{\frac{\Delta t^2}{4} + 4 \times 1 \times \frac{\Delta t^2}{4}}}{2} = \frac{\frac{\Delta t}{2} \pm \frac{1}{2}\sqrt{5\Delta t^2}}{2}$$

$$t = \frac{\Delta t}{4} \pm \sqrt{5\Delta t} / 4$$

$$= \frac{\Delta t}{4} \pm \frac{\sqrt{5\Delta t}}{4}$$

$$= \frac{\Delta t}{4} (1 \pm \sqrt{5})$$

EV  $t < \Delta t$  ✓

3.92

GS

Const acc<sup>n</sup> problem  $S = ut + \frac{1}{2}at^2$

DI

Find expression for time of flight.

Write expression for dist. travelled in last s.

Ex.  $h = \frac{g}{2} t^2$   $t = \sqrt{\frac{2h}{g}}$

~~In last second~~ Up to last second ( $t \rightarrow 0$  ... 1s before impact)

$$(h - 2g) = 0 + \frac{g}{2} \left( \sqrt{\frac{2h}{g}} - 1 \right)^2$$

$$\frac{2h - 58}{g} = \left( \sqrt{\frac{2h}{g}} - 1 \right)^2$$

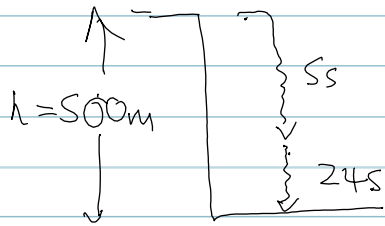
$$\frac{-\frac{58}{g} - 1}{-2} = \sqrt{\frac{2h}{g}}$$

$$\left( \frac{58}{2g} + \frac{1}{2} \right)^2 = \frac{2h}{g}$$

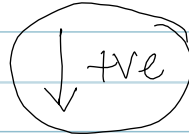
$$h = \frac{g}{2} \times \left( \frac{58}{2g} + \frac{1}{2} \right)^2 = \boxed{59\text{m}}$$

EV

3.108



$$a = 0.64g$$



Const acc<sup>n</sup> problem.

DP ① Dist fallen is 5s.

$$s = ut + \frac{1}{2}at^2$$

② Calc. speed at this point

$$v = u + at$$

③ Calc new acc<sup>n</sup> using jet pack

$$s = ut + \frac{1}{2}at^2$$

④ Final landing speed.

$$\rightarrow v = u + at$$

$$\textcircled{1} \quad s = 0 + \frac{1}{2} \frac{64}{100} g t^2$$

$$s = \underline{78.4m}$$

$$\textcircled{2} \quad v = 0 + \frac{64}{100} g t = \underline{31.4 \text{ ms}^{-1}}$$

③ After jet pack fires

$$(500 - s) = (v \times 24) + \frac{1}{2} a' \times 24^2$$

$$a = \underline{-1.15 \text{ ms}^{-2}} \quad \uparrow$$

$$\textcircled{4} \quad v' = v - 1.15 \times 24$$

$$= \boxed{3.77 \text{ ms}^{-1}}$$

downwards.