

a) A.M. about c of m of barbell (its initial position)

$$m v_i \frac{4d}{5} = m v_f \frac{4d}{5} \cos \theta + m \left(2\pi \frac{4d}{5T} \right) \frac{4d}{5} + 4m \left(2\pi \frac{d}{5T} \right) \frac{d}{5}$$

Cancel $\frac{md}{5}$ everywhere.

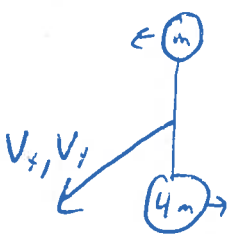
$$4v_i = 4v_f \cos \theta + \frac{2\pi}{T} \frac{16d}{5} + \frac{2\pi}{T} \frac{4d}{5}$$

$$v_i - v_f \cos \theta = \frac{2\pi d}{T}$$

$$T = \frac{2\pi d}{v_i - v_f \cos \theta}$$

①

b) K.E. immediately after the collision:



$$\text{for } m: v_x = v_x + 2\pi \frac{4d}{5T} \quad v_y = v_y$$

$$\text{for } 4m: v_x = v_x - 2\pi \frac{d}{5T} \quad v_y = v_y$$

$$\text{so } K.E. = \frac{1}{2} m \left[\left(v_x + 2\pi \frac{4d}{5T} \right)^2 + v_y^2 \right] + \frac{1}{2} (4m) \left[\left(v_x - 2\pi \frac{d}{5T} \right)^2 + v_y^2 \right]$$

$$KE = \frac{1}{2} m \left[V_x^2 + V_y^2 + \frac{4\pi d}{5r} V_x + 16 \left(\frac{2\pi d}{5r} \right)^2 \right] + \frac{1}{2} (4m) \left[V_x^2 + V_y^2 - \frac{4\pi d}{5r} V_x + \left(\frac{2\pi d}{5r} \right)^2 \right]$$

$$KE = \frac{1}{2} (5m) (V_x^2 + V_y^2) + \frac{2}{5} \left(\frac{2\pi d}{r} \right)^2 m$$

c) Cons E:

$$\frac{1}{2} m v_i^2 = \frac{1}{2} m v_f^2 + \frac{1}{2} (5m) (V_x^2 + V_y^2) + \frac{2}{5} \left(\frac{2\pi d}{r} \right)^2 \quad (2)$$

$$\text{Cons } p_x: m v_i = m v_f \cos \theta + 5m V_x \rightarrow v_i - v_f \cos \theta = 5 V_x \quad (3)$$

$$\text{Cons } p_y: m v_f \sin \theta = 5m V_y \rightarrow V_y = \frac{v_f \sin \theta}{5} \quad (4)$$

plus (1), (3) and (4) into (2) to eliminate $\frac{2\pi d}{r}$, V_x , V_y

$$\frac{1}{2} m v_i^2 = \frac{1}{2} m v_f^2 + \frac{1}{2} (5m) \left[\left(\frac{v_i - v_f \cos \theta}{5} \right)^2 + \left(\frac{v_f \sin \theta}{5} \right)^2 \right] + \frac{2}{5} (v_i - v_f \cos \theta)^2 m$$

$$5 v_i^2 = 5 v_f^2 + \left[v_i^2 - 2 v_i v_f \cos \theta + v_f^2 \cos^2 \theta + v_f^2 \sin^2 \theta \right] + 4 (v_i^2 - 2 v_i v_f \cos \theta + v_f^2 \cos^2 \theta)$$

$$0 = 6 v_f^2 - 10 v_i v_f \cos \theta + 4 v_f^2 \cos^2 \theta$$

$$v_f (3 + 2 \cos^2 \theta) = 5 v_i \cos \theta$$

$$v_f = \frac{5 v_i \cos \theta}{3 + 2 \cos^2 \theta}$$